

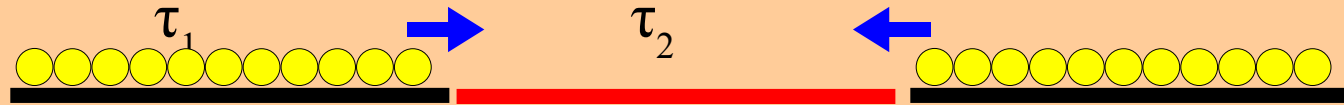
Stripe formation close to a critical point: Au on W(110)

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Stress-domain self-assembly

Competition between cost of making boundaries, and elastic interaction between the boundaries deforming the substrate and **lowering** the energy:

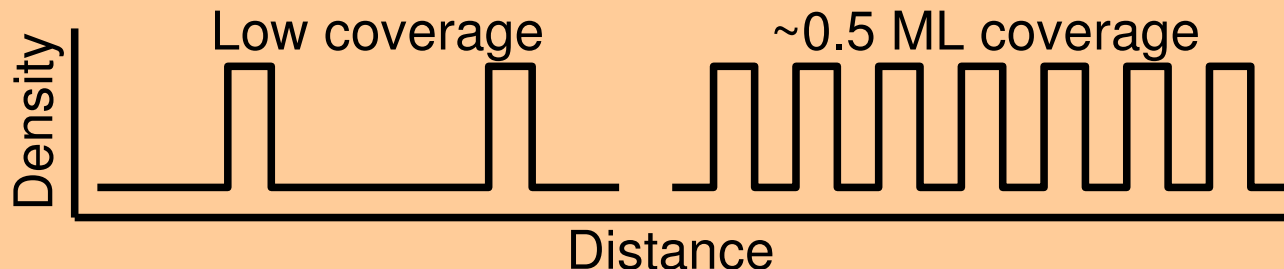


- ➡ Total energy per unit length of an array of domains, including the boundary energy,

$$E(l) = C_{\text{boundary}} - C_{\text{elastic}} \ln\left(\frac{2l}{\pi a}\right)$$

- ➡ There is a preferred length

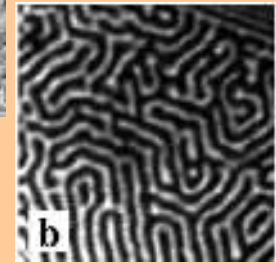
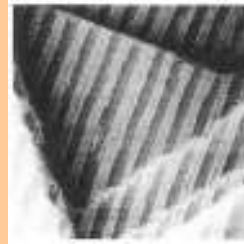
$$l_0 = \frac{\pi a}{2} e^{\frac{C_{\text{elastic}}}{C_{\text{boundary}}} + 1}$$



Stress domains for self-assembly of patterns on surfaces

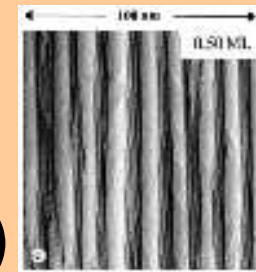
→ Flat domains:

- O/Cu{110}-(2x1)O
- Si(100): original motivation
- Pb/Cu(111): best example so far



→ Faceted Surfaces:

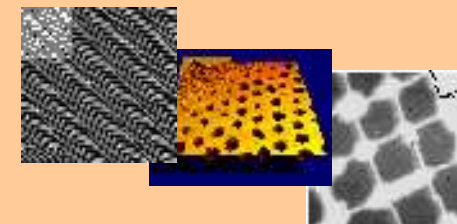
- Au(111) vicinals
- Ag-induced faceting of Cu(111)



P. Zeppenfeld et al., *Phys. Rev. Lett.* **72** (1994) 2737
O.L. Alerhand et al., *Phys. Rev. Lett.* **64**, (1990) 2406
S. Rousset et al., *Surf. Sci.* **422** (1999) 33
A. R. Bachmann et al., *Surf. Sci.* **526** (2003) L143
R. Plass et al., *Nature* **412**, (2001) 875
R. van Gastel et al., *Phys. Rev. Lett.* **91** (2003) 055503

And some cases where it was assumed:

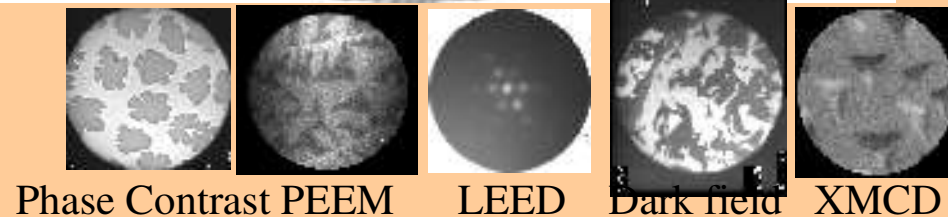
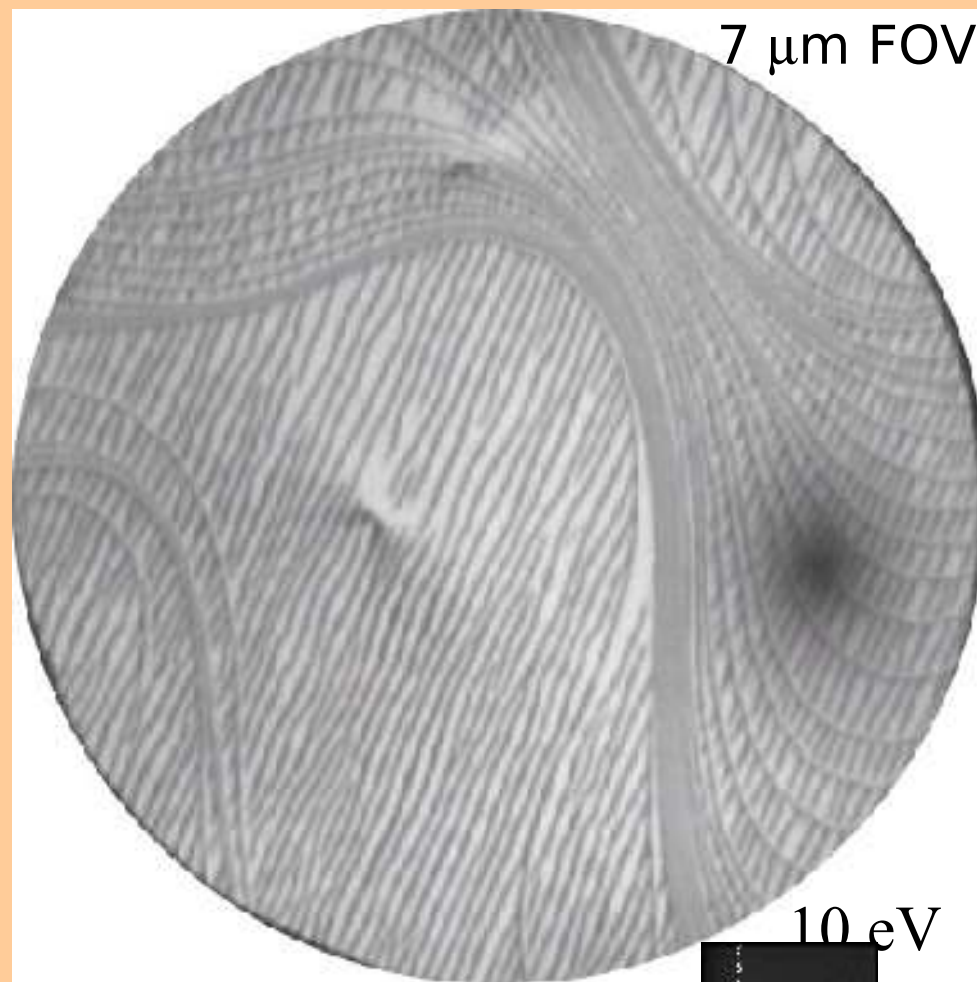
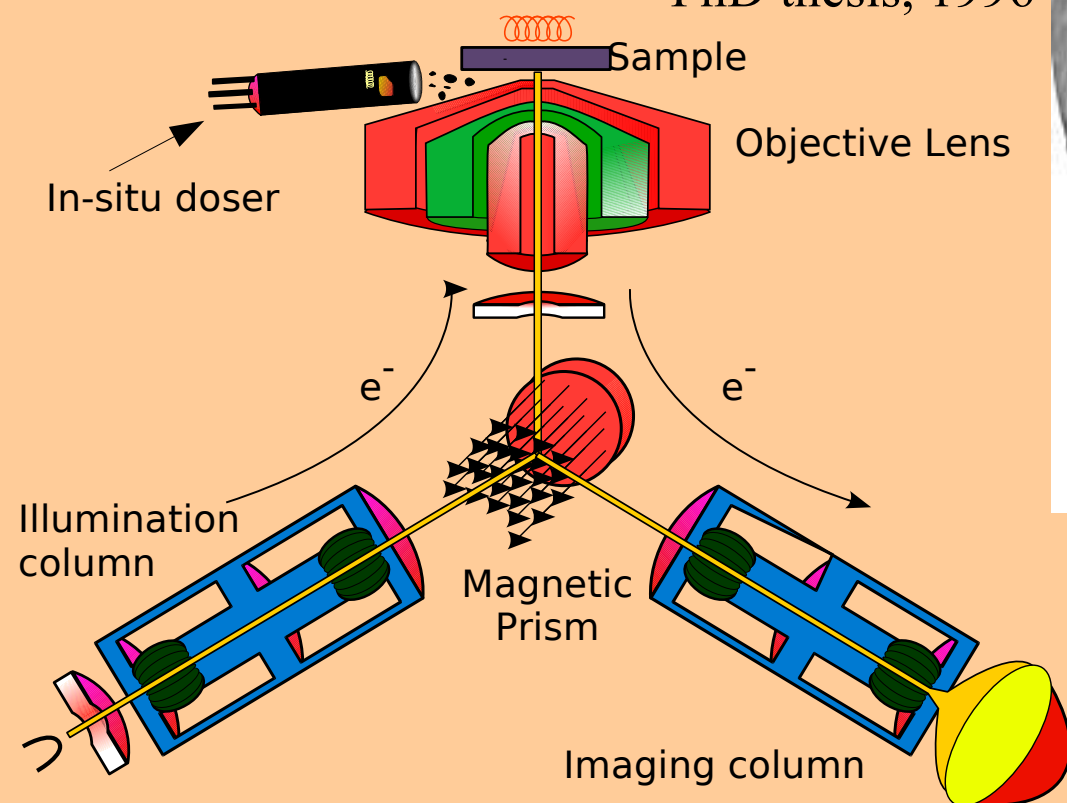
- Au(111) herringbone
- S/Ag/Ru(0001)
- N/Cu(100)



Stripes on Au/W(110) observed by LEEM

- ➔ A very simple system:
- ➔ Deposit Au at the appropriate temperature
- ➔ First reported by Thomas Duden and Ernst Bauer*

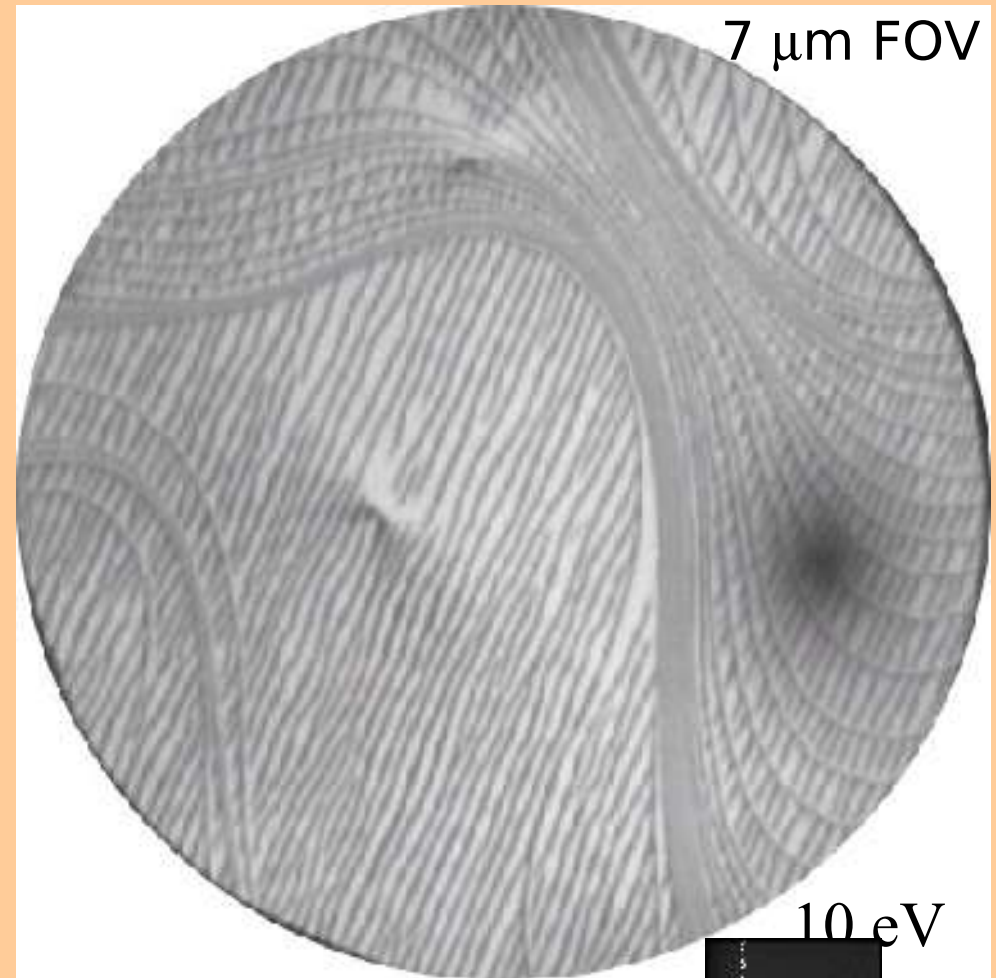
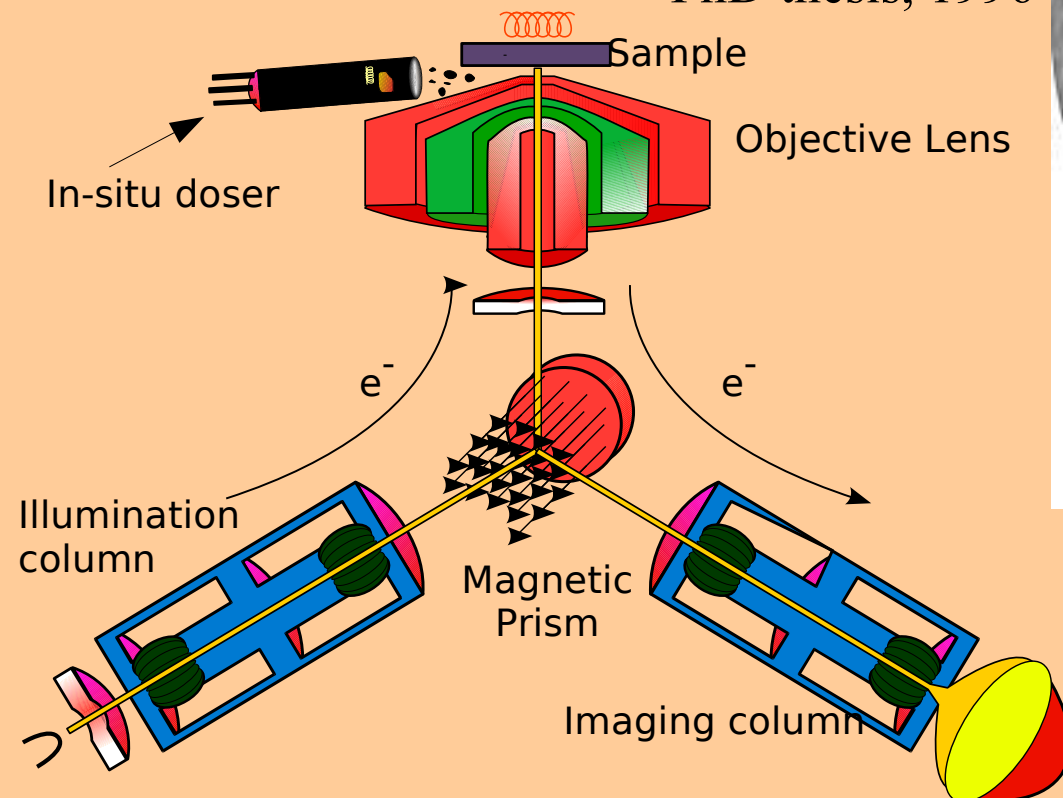
*PhD thesis, 1996



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Phase Contrast PEEM LEED Dark field XMCD

Do the deposition at a higher temperature: breaking up the standard model

7 μm FOV

Unlike at lower temperatures, the periodicity does not seem to change much!



Do the deposition at a higher temperature: breaking up the standard model

7 μm FOV

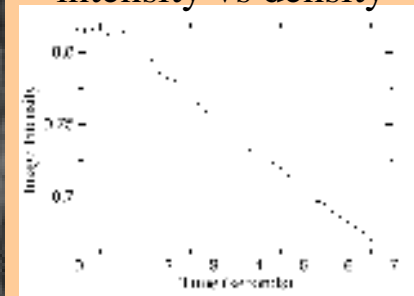
Unlike at lower temperatures, the periodicity does not seem to change much!



Evolution with coverage

calibrating

intensity vs density



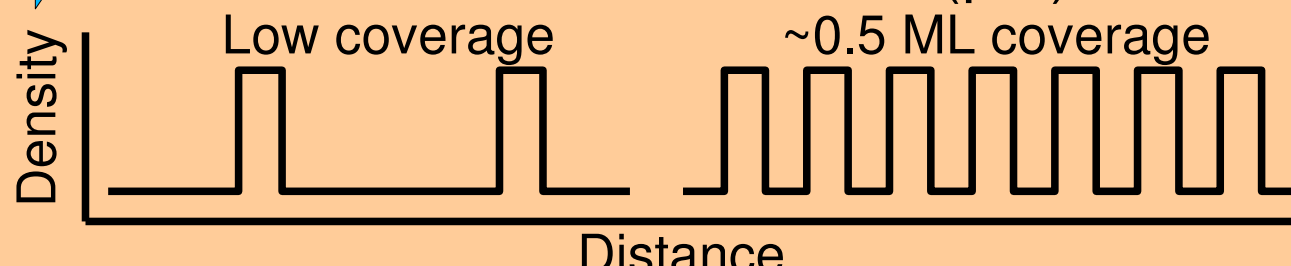
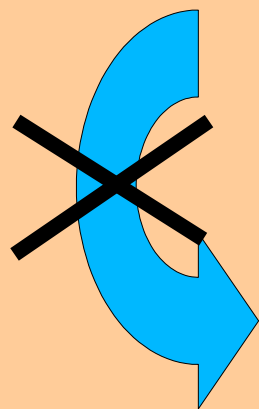
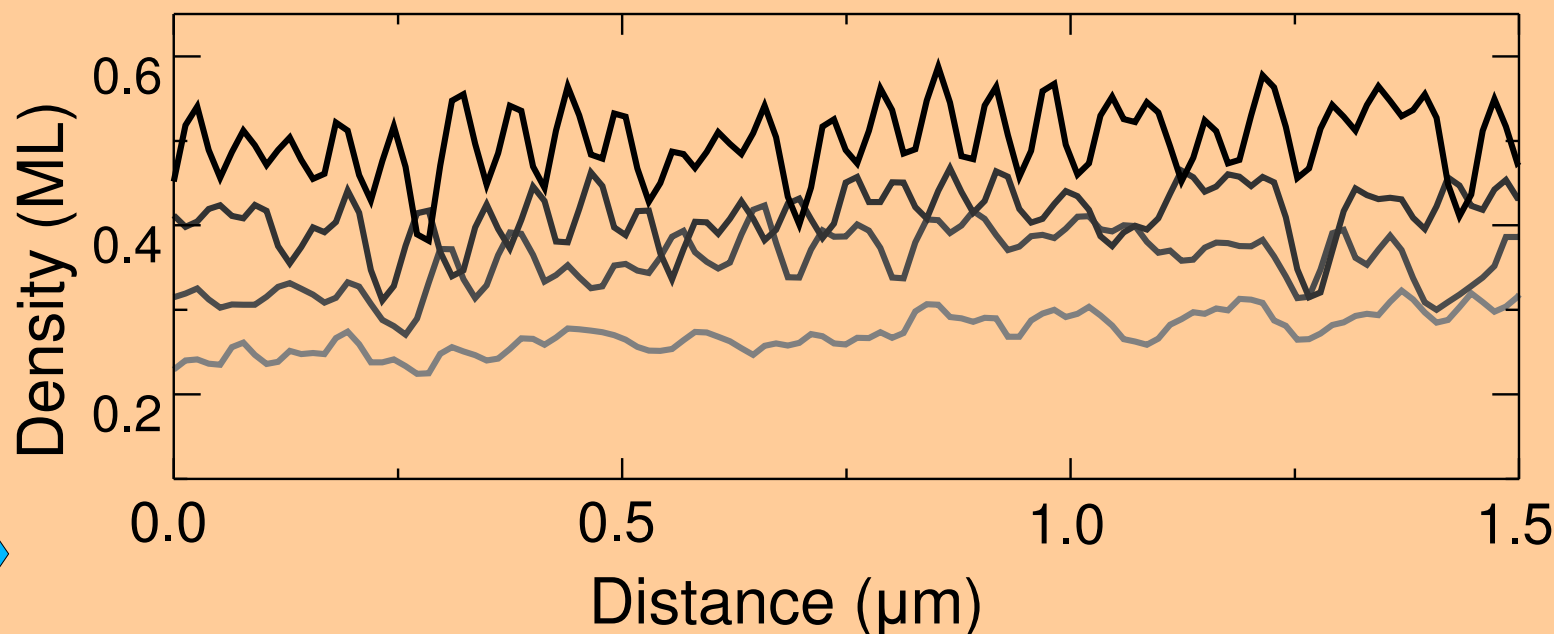
cond-
mat/0601406

0.26 ML

0.35 ML

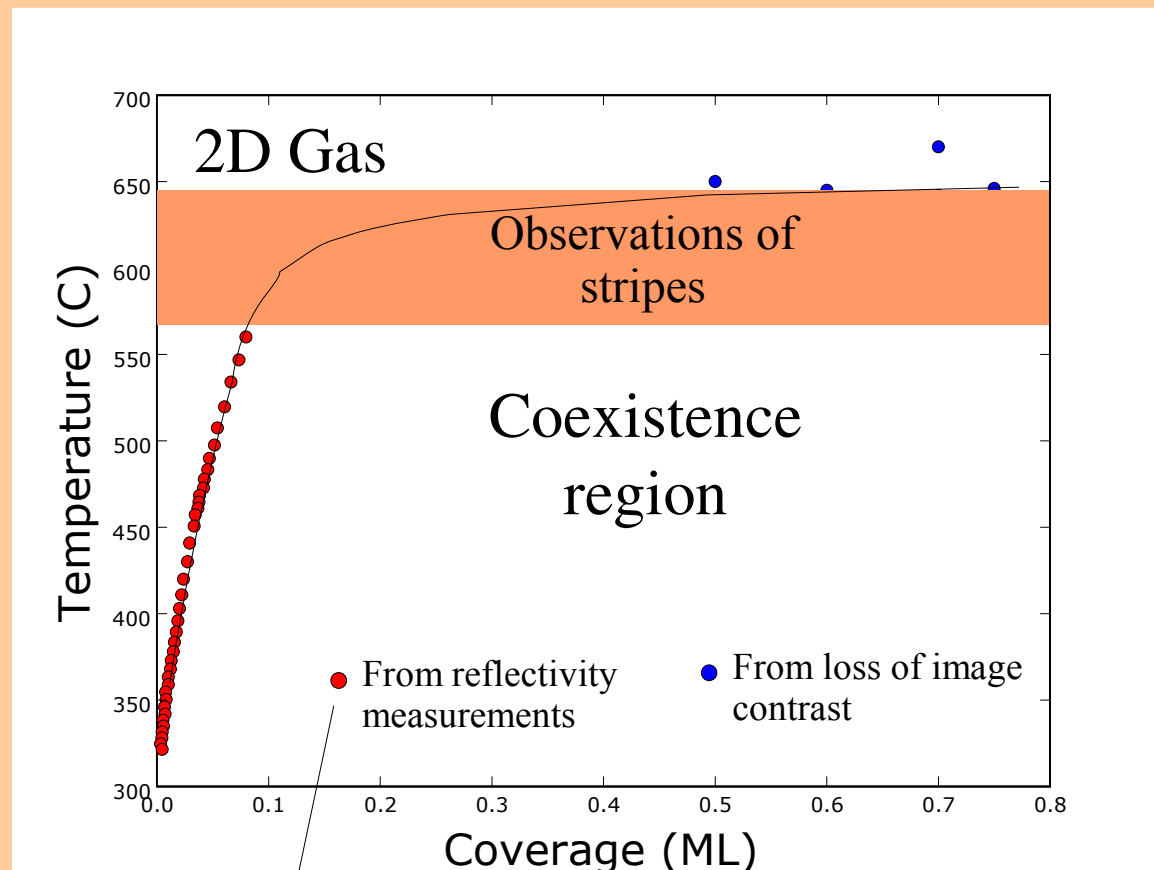
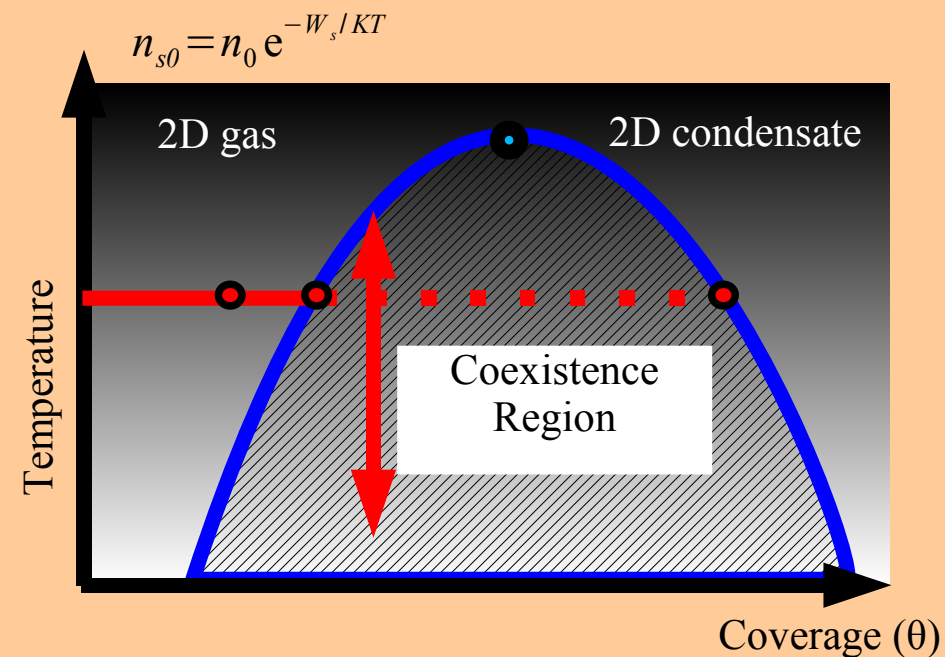
0.42 ML

0.51 ML



We are close to the critical point...

Typical 2D phase diagram



J. Kolaczkiwicz and E. Bauer, *Surf. Sci.* **155** (1985) 700
 J. Kolaczkiwicz and E. Bauer, *Surf. Sci.* **151** (1985) 333

Juan de la Figuera, Norm C Bartelt, Kevin F McCarty,
Surf. Sci. **600** (2006) 4062 cond-mat/0601406

<http://surfmoss.iqfr.csic.es>

What is the problem?

- Up to now, we are assuming we have sharp boundaries:

- compact condensed gold phase
- empty space between them

$$\lambda \approx e^{\frac{C_{\text{boundary}}}{C_{\text{elastic}}}}$$

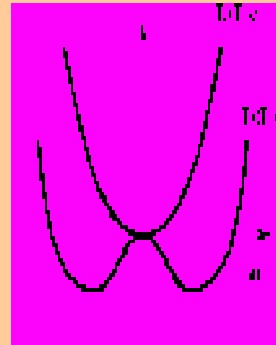
Au

Au

W(110)

- But as we are not so far from the critical point, nothing is so distinct:

- we have a dense adatom gas in between (0.2 ML!), separated by not-so-compact condensed Au
- use a continuum model, with variable density $\phi = (2\rho - \rho_0)/\rho_0$



Critical point

Elastic interaction

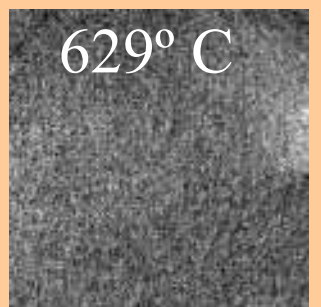
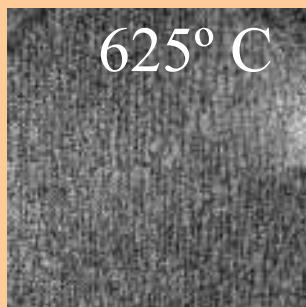
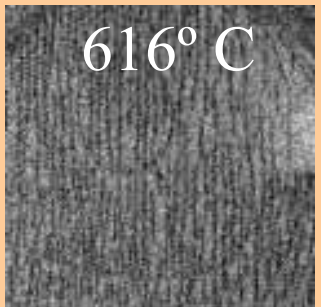
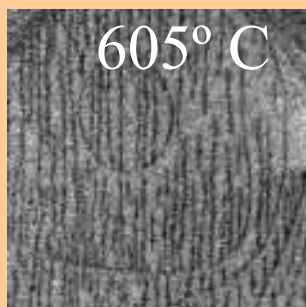
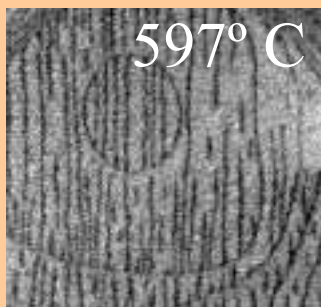
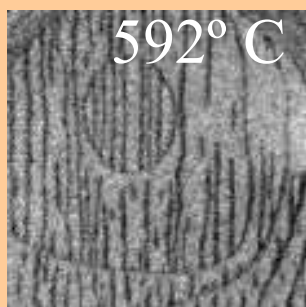
$$f[\phi(x)] = \int dx \left[-\frac{r}{2}\phi^2 + \frac{u}{4}\phi^4 + \frac{c}{2}|\nabla\phi|^2 \right] + g \int \int dx dx' \frac{\phi(x)\phi(x')}{(x-x')^2 + a^2}$$

Cost of boundaries



W(110)

Change the temperature

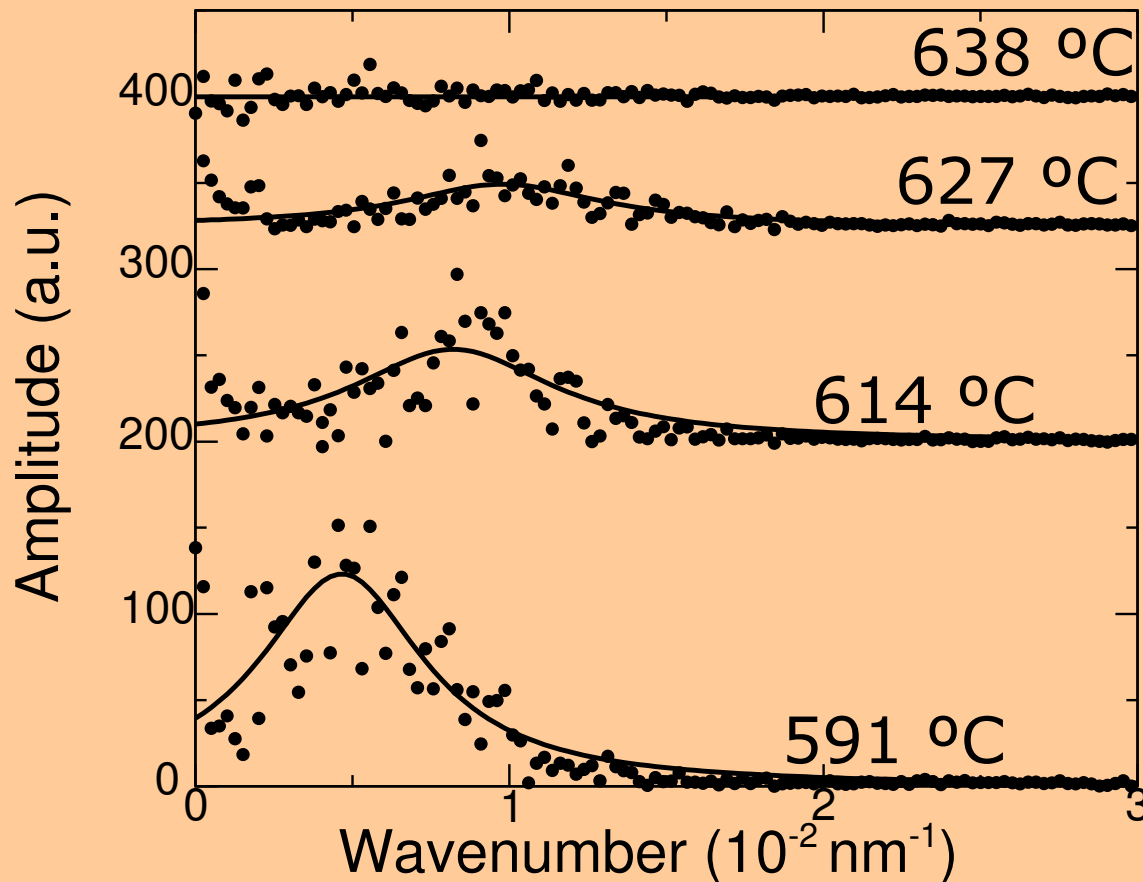
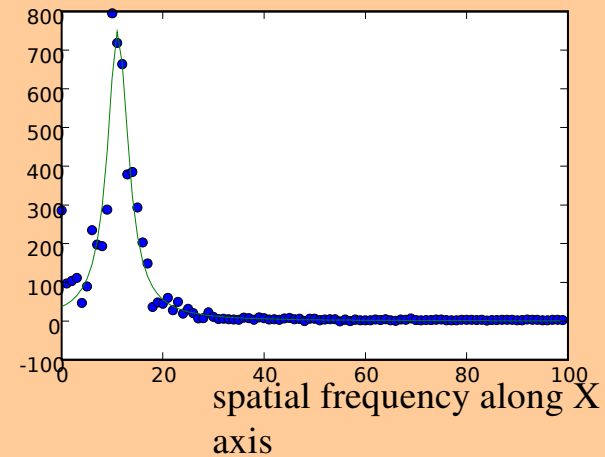
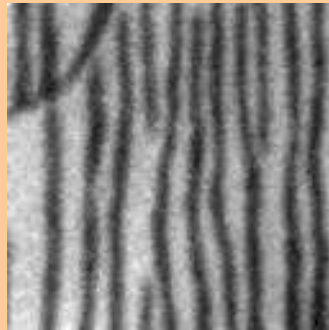
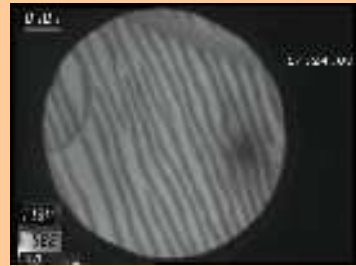


7 μm FOV



TEMPERATURE $\Rightarrow$

Measuring the pattern periodicity



To extract stripe period from movie (between 20k and 30k frames):

- Rotate image (extract center area)
- Subtract background (unfocused)
- Perform a 2D FFT
- Extract a profile along k_x ($k_y=0$)
- Average as many profiles as desired
- Fit the result to a lorentzian

Limiting value of stripe periodicity!

Amplitude vs temperature: decreases steadily

Periodicity vs temperature: reaches a constant value

For the **diffuse boundary model**, assuming a sinusoidal profile at high T:
 $\phi(x) = A \cos(2\pi/\lambda_c)$

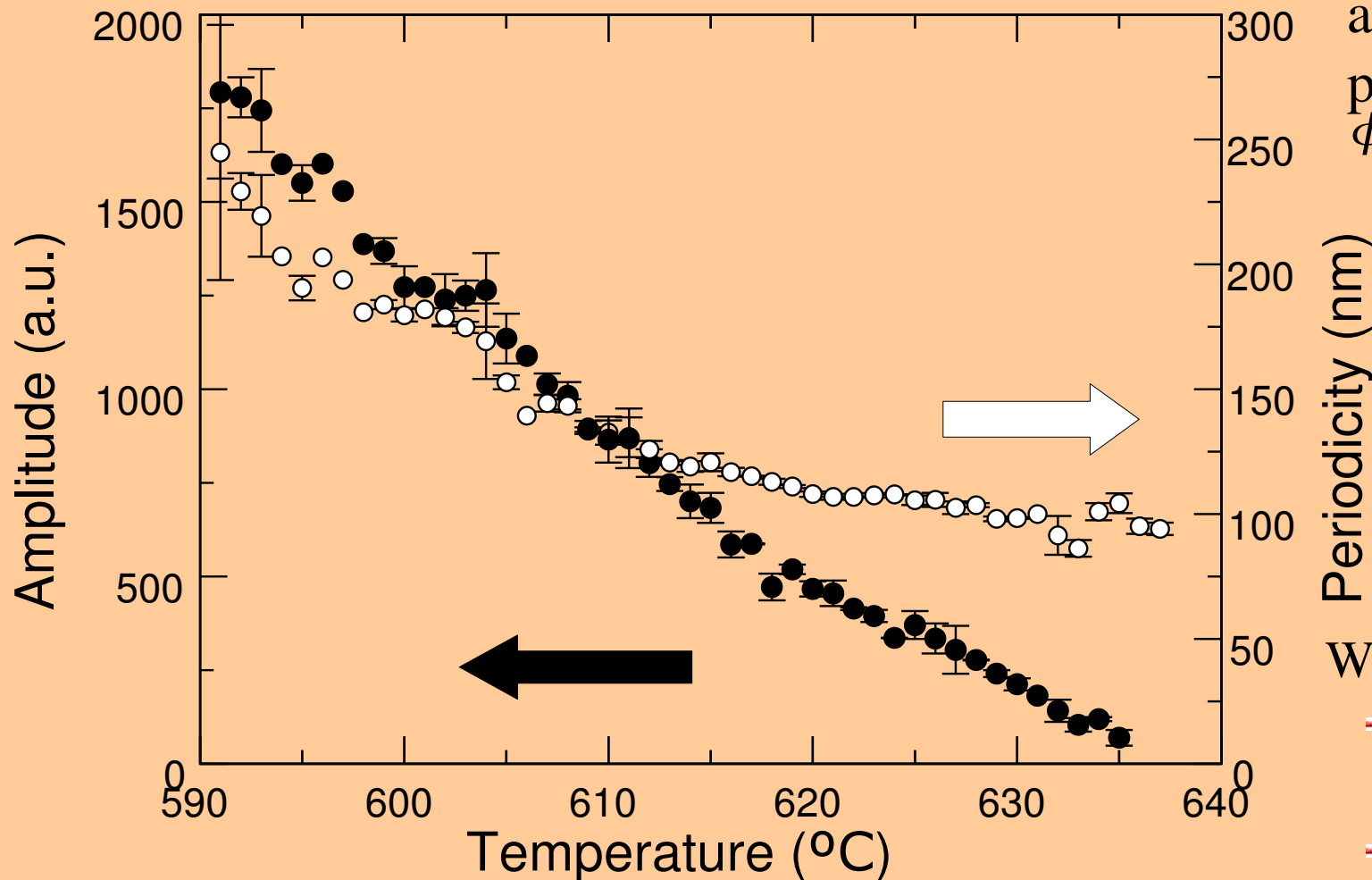


$$\lambda_c = \frac{\gamma_c}{g} \neq .$$

We need an estimate of:

- short range interaction
- long range (elastic) interaction

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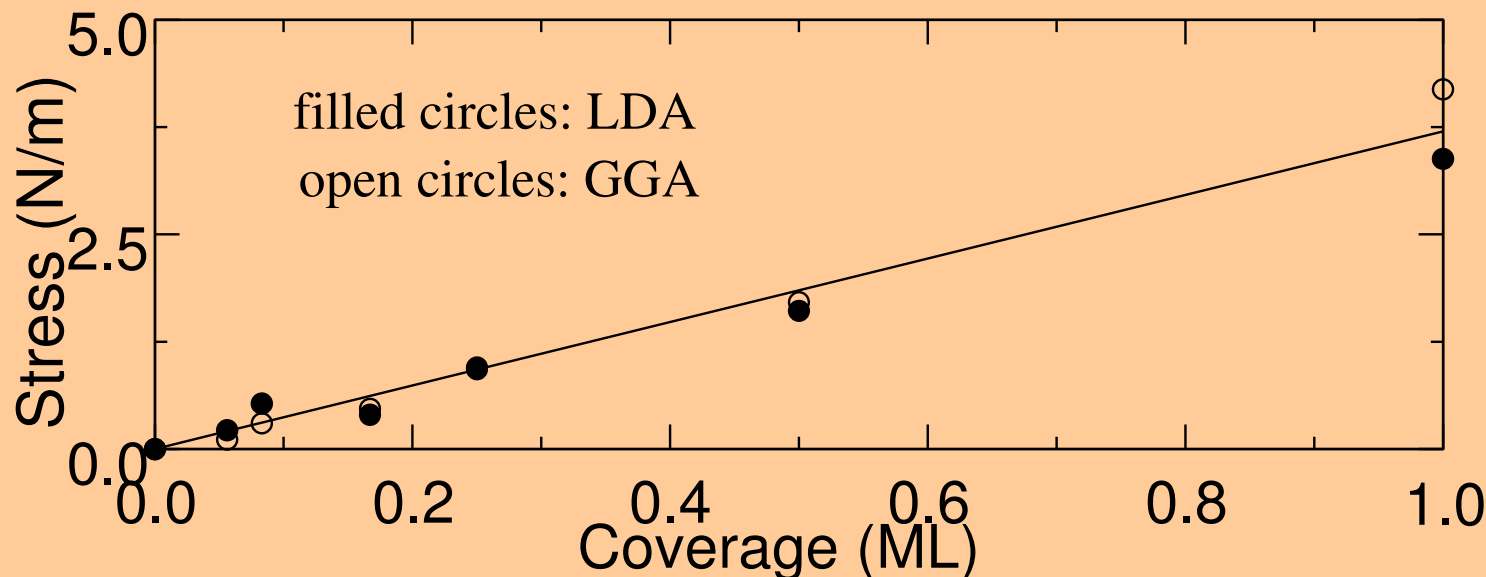


Long range elastic interaction

- ➡ Use DFT (VASP) to compute the (excess) surface stress as a function of Au coverage... $\Delta\tau$
- ➡ Use (non-isotropic!) elasticity theory to estimate the interaction for a given stress difference given the Au/W(110) stripes orientation: M

F. Leonard, N. C. Bartelt, and G. L. Kellogg,
Phys. Rev. B **71**, 045416 (2005).

$$g = (\Delta\tau)^2 M / 2\pi = 9.8 \times 10^{-12} \text{ J/m}$$



Short range interaction

- ➡ Study how stripe periodicity and amplitude change when approaching T_c
 - ➡ Extend the previous one-mode analysis to two modes
- ➡ Stripe periodicity close to T_c :

$$\lambda = \lambda_c \left[1 + \frac{\lambda_c^2}{3\lambda\xi\pi^4} \left(\frac{a^2 r_0 T_c}{c} \right)^2 \left(1 - \frac{T}{T_c} \right)^2 \right]$$

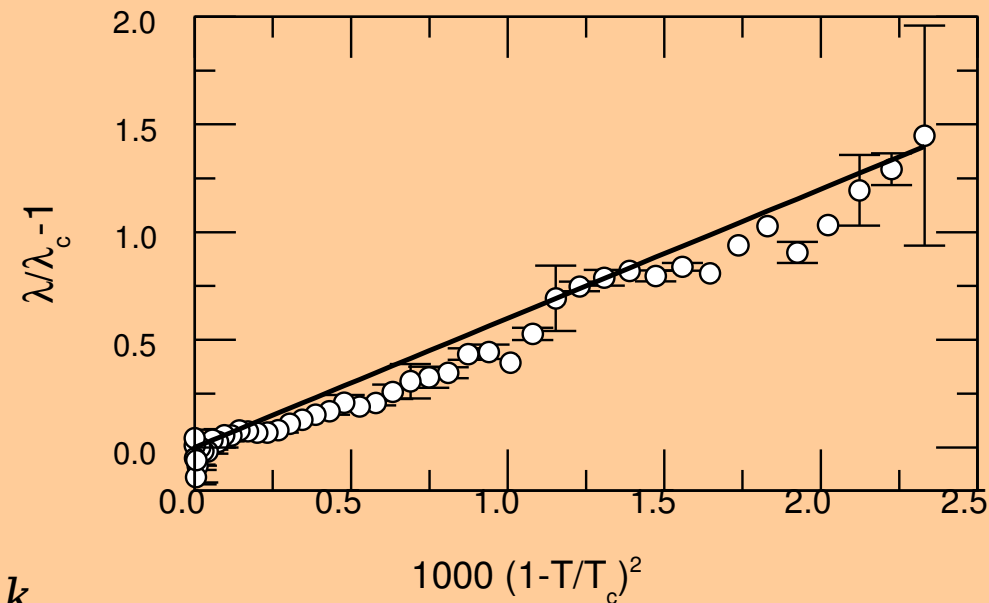
$\frac{a^2 r_0 T_c}{c} \approx 0.5$

J. W. Cahn and J. E. Hillard, *J. Chem. Phys.* **28**, 258 (1958)

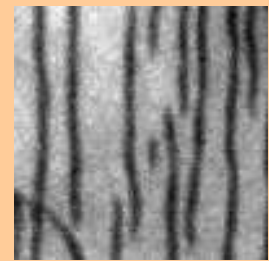
$$a^2 r_0 = 4k_B$$

By fitting the previous dependence, we obtain $c \approx 8k_B T_c$

$$\lambda_{c, theory} = \frac{2c}{g} \approx 20 \text{ nm}$$



Summary



- ➡ We have characterized the stripe formation of Au on W(110):
 - ➡ Observations at high T are incompatible with the sharp-boundary model
 - ➡ Non-constant density in components of stripes
 - ➡ Limiting value of periodicity
- ➡ The results can be understood within a model *with diffuse boundaries*:
 - ➡ The prediction is a linear dependence on material properties

We expect modulated patterns to be prevalent close to critical points at surfaces!!

The people that does the work!

and the theory people

Norm C. Bartelt

the experimentalists

Roland Stumpf



Francois Leonard



Kevin F. McCarty



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arxiv 0804.1273, accepted Phys. Rev. Lett.

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